

ANSWERS TO POWER SERIES ESTIMATION FOR A DEFINITE INTEGRAL EXPLORATION

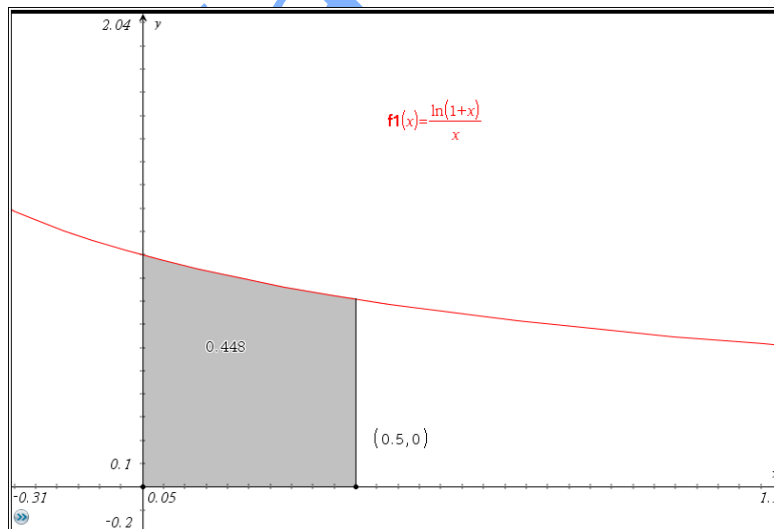
1. $\frac{\ln(1+x)}{x} = 1 - \frac{x}{2} + \frac{x^2}{3} - \frac{x^3}{4} + \frac{x^4}{5} - \dots$

2, 3, 4 & 5:

$\int_0^{0.5} \left(1 - \frac{x}{2} + \frac{x^2}{3} - \frac{x^3}{4}\right) dx$	0.447483
$\int_0^{0.5} \frac{\ln(1+x)}{x} dx$	0.448414
$0.44841420692383 - 0.44748263888889$	0.000932
$\frac{(0.5)^5}{25}$	0.00125

The approximation is correct to 2 decimal places when using the first four terms. The absolute value of the error is less than the first unused term $\frac{x^5}{25}$, which evaluates to 0.00125.

The error is 0.000932 which is in agreement with the Alternating Series Estimation Theorem.



6. The series $\ln(1+x) = \sum_{k=1}^{\infty} (-1)^{k+1} \frac{x^k}{k} = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$ converges for $-1 < x \leq 1$ so we cannot approximate the area which goes beyond this interval.

1.1 1.2 *Unsaved

$\int_0^2 \left(1 - \frac{x}{2} + \frac{x^2}{3} - \frac{x^3}{4} \right) dx$ 0.888889

$\int_0^2 \frac{\ln(1+x)}{x} dx$ 1.43675

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Mathexams